

Inspector Clauseau → slide 34 Lecture 1

$$P(B|K) = \frac{P(B, K)}{P(K)} \quad \text{definition cond. prob}$$

$$= \frac{\sum_M P(K, B, M)}{\sum_{B, M} P(K, B, M)} \quad \text{marginalization}$$

remark that

$$P(K, B, M) = P(K|B, M) P(B, M) \quad (\text{def. cond. prob})$$

~~$P(K|B, M) P(B) P(M)$~~ (assumed independence)

$$P(B|K) = \frac{\sum_M P(K|B, M) P(B) P(M)}{\sum_B \sum_M P(K|B, M) P(B) P(M)}$$
$$= \frac{P(B) \sum_M P(K|B, M) P(M)}{\sum_B P(B) \sum_M P(K|B, M) P(M)}$$

$$\text{so } P(B=m | K=R) = \frac{P(B=m) \sum_M P(K=R | B=m, M) P(M)}{\sum_B P(B) \sum_M P(K=R | B, M) P(M)}$$

$$= \frac{P(B=m) [P(K=R | B=m, M=m) P(M=m) + P(K=R | B=m, M=nm) P(M=nm)]}{P(B=nm) [P(K=R | B=nm, M=m) P(M=m) + P(K=R | B=nm, M=nm) P(M=nm)]}$$

$$= \frac{\frac{6}{10} \left[\frac{1}{10} \times \frac{2}{10} + \frac{6}{10} \times \left(1 - \frac{2}{10}\right) \right]}{\frac{6}{10} \left[\frac{1}{10} \times \frac{2}{10} + \frac{6}{10} \times \left(1 - \frac{2}{10}\right) \right]} = 0.728 \dots$$

$$= \frac{1 - \frac{6}{10} \left[\frac{2}{10} \times \frac{2}{10} + \frac{3}{10} \times \left(1 - \frac{2}{10}\right) \right]}{\dots}$$